



Evidence for Multiple Accretion Events in the Gaia-Sausage/Enceladus Structures

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Abstract

We present evidence that multiple accretion events are required to explain the origin of the Gaia-Sausage and Enceladus (GSE) structures, based on an analysis of dynamical properties of main-sequence stars from the Sloan Digital Sky Survey Data Release 12 and Gaia Data Release 2. GSE members are selected to have eccentricity (e) > 0.7 and $[\text{Fe}/\text{H}] < -1.0$, and separated into low and high orbital-inclination (LOI/HOI) groups. We find that the LOI stars mainly have $e < 0.9$ and are clearly separable into two groups with prograde and retrograde motions. The LOI stars exhibit prograde motions in the inner-halo region and strong retrograde motions in the outer-halo region (OHR). We interpret the LOI stars in these regions to be stars accreted from two massive dwarf galaxies with low-inclination prograde and retrograde orbits, affected to different extents by dynamical friction due to their different orbital directions. In contrast, the majority of the HOI stars have $e > 0.9$, and exhibit a globally symmetric distribution of rotational velocities (V_ϕ) near zero, although there is evidence for a small retrograde motion for these stars ($V_\phi \sim -15 \text{ km s}^{-1}$) in the OHR. We consider these stars to be stripped from a massive dwarf galaxy on a high-inclination orbit. We also find that the LOI and HOI stars on highly eccentric and tangential orbits with clear retrograde motions exhibit different metallicity peaks at $[\text{Fe}/\text{H}] = -1.7$ and -1.9 , respectively, and argue that they are associated with two low-mass dwarf galaxies accreted in the OHR of the Galaxy.

Unified Astronomy Thesaurus concepts: Milky Way stellar halo (1060); Stellar kinematics (1608); Stellar dynamics (1596); Milky Way Galaxy (1054); Stellar abundances (1577); Stellar populations (1622); Surveys (1671)

1. Introduction

The studies of the stellar halo of the Milky Way (MW), which is thought to be assembled via multiple hierarchical mergers (White & Frenk 1991), provide valuable clues to its formation and evolutionary history, as its long dynamical timescale preserves a fossil record of past accretion events (Bland-Hawthorn & Gerhard 2016). The advent of the Gaia Data Releases (Gaia DRs; Gaia Collaboration et al. 2016, 2018), which provide precise astrometric information for many millions of stars, has dramatically expanded the detail of our view of the MW's accretion history. For instance, the combination of Gaia and large spectroscopic survey data has enabled the detection of distinctive accretion signatures from the Gaia-Sausage (GS; Belokurov et al. 2018) and Gaia-Enceladus (GE; Helmi et al. 2018). Other small-scale accretion events have also been discovered (Myeong et al. 2018, 2019; Koppelman et al. 2019; Naidu et al. 2020; Necib et al. 2020; Yuan et al. 2020; Horta et al. 2021; Re Fiorentin et al. 2021).

According to the study of Belokurov et al. (2018), who used a sample of main-sequence (MS) stars from the Sloan Digital Sky Survey (SDSS; York et al. 2000) along with Gaia DR1 astrometry, the GS structure exhibits strong radial anisotropy and a mildly prograde motion of $20 \sim 30 \text{ km s}^{-1}$ for stars with $-1.7 < [\text{Fe}/\text{H}] < -1.0$. Based on cosmological zoom-in simulations of the formation of the stellar halo, they argued that the GS is the result of an accretion event of a massive dwarf galaxy with orbital eccentricity $e > 0.9$. From a sample of nearby MS and blue horizontal-branch stars with SDSS DR9 (Ahn et al. 2012) spectroscopy and Gaia DR2 proper motions, Deason et al. (2018) demonstrated that the GS stars with $-1.5 < [\text{Fe}/\text{H}] < -1.0$ have eccentricities $e > 0.9$ in the range of $10 < r_{\text{max}}$ (apogalactic distance) $< 30 \text{ kpc}$, and an average r_{max}

agrees with the break radius of the MW stellar halo (Deason et al. 2013).

From an analysis of the kinematics, chemical abundances, ages, and spatial distributions of disk and halo stars in Gaia DR2 with available spectroscopy from the Apache Point Observatory Galactic Evolution Experiment (APOGEE) DR14 (Majewski et al. 2017; Abolfathi et al. 2018), Helmi et al. (2018) identified that GE stars primarily occupy the inner-halo region (IHR), and exhibit a small retrograde net motion. They also suggested that the GE stars are debris from a massive dwarf galaxy, inferred from their relatively low $[\alpha/\text{Fe}]$ and a large spread in metallicity. Mackereth et al. (2019) additionally found a robust correlation between the chemical abundances and the orbital eccentricities of local halo stars using the APOGEE DR14 data. Their results indicated that the majority of local halo stars have highly radial orbits with $e > 0.7$ (see also Mackereth & Bovy 2020), and relatively low abundances of $[\text{Mg}/\text{Fe}]$, $[\text{Al}/\text{Fe}]$, and $[\text{Ni}/\text{Fe}]$, which are comparable to those of stars observed in massive surviving satellite galaxies of the MW.

The general consensus of the above studies is that both the GS and GE stars exhibit eccentric and radial orbits in the inner halo, and they are possibly the remnants of a single massive ($\sim 10^9 M_\odot$) disrupted galaxy. Nonetheless, closer inspection has suggested that they have different rotational motions, and that the GS stars appear to have $e > 0.9$, higher than the GE stars (Belokurov et al. 2018; Deason et al. 2018; Helmi et al. 2018; Mackereth et al. 2019). Thus, it is still an open question whether or not the GS and GE stars have originated from a single accretion event.

Recent studies have demonstrated that the dynamical properties of likely progenitors for different substructures can be a powerful tool to distinguish one accretion episode from another. For example, studies of minor-merging simulations (Read et al. 2008; Villalobos & Helmi 2008; Jean-Baptiste

et al. 2017; Karademir et al. 2019) showed that the key ingredients of merged galaxies to understand the orbits of stripped stars are their orbital eccentricity, inclination, and inferred mass. In particular, the orbital eccentricities of disrupted stars largely remain unchanged after accretion (Mackereth et al. 2019), and the majority of these stars orbit with the same orbital inclinations as of their parent galaxies (Re Fiorentin et al. 2015).

Retrograde motions of stars in the outer halo of a galaxy have been shown by merging simulations to arise from dwarf parent galaxies on low-inclination retrograde orbits (Bignone et al. 2019). Two massive dwarf galaxies with different orbital directions on high-eccentricity orbits (Murante et al. 2010) can also produce stars with retrograde motions. Observations also confirm these predictions by various simulations. Helmi et al. (2018) found, from isolated simulations of minor mergers (e.g., Villalobos & Helmi 2009), that the retrograde motion of the GE stars is similar to that of a retrograde encounter with a low-inclination dwarf. In addition, Simion et al. (2019) verified that the Hercules-Aquila cloud and Virgo overdensity are dominated by stars on highly eccentric orbits, which are commensurate with the kinematic and orbital properties of the GS stars. They also showed that both of the diffuse debris clouds associated with this structure have high orbital-inclination trajectories. These studies imply that dwarf galaxies with different orbital inclination leave distinct dynamical signatures in their disrupted stars; thus the orbital inclination of their disrupted stars can be used to trace the orbital properties of their progenitors.

Following the above reasoning, in this Letter we first identify two groups of stars—low orbital-inclination (LOI) and high orbital-inclination (HOI) stars—among stars with high eccentricity ($e > 0.7$) and $[\text{Fe}/\text{H}] < -1.0$, the typical properties of the GS and GE (GSE, hereafter) stars, and report on the distinct chemical and dynamical signatures of LOI and HOI groups, providing strong evidence for multiple accretion events involved in the formation of the GSE structures.

This Letter is organized as follows. We explain our sample selection in Section 2, and calculations of velocity components and orbital parameters of our sample stars in Section 3. In Section 4, we examine kinematic and orbital properties of LOI and HOI stars in the IHR, and present evidence for accretion events that are distinct from the GSE structures, as well as the identification of retrograde motions associated with stars in the outer-halo region (OHR). Section 5 discusses the implications of our findings; a summary follows in Section 6.

2. Selection of Sample Stars

We have collected a sample of stars with available medium-resolution ($R \sim 2000$) spectra from SDSS DR12 (Alam et al. 2015), which includes objects from the legacy SDSS program, the Sloan Extension for Galactic Understanding and Exploration (SEGUE; Yanny et al. 2009), and the Baryon Oscillation Spectroscopic Survey (BOSS; Dawson et al. 2013), covering the extinction-corrected magnitude and dereddened color ranges $14.0 < g_0 < 20.0$ and $0.0 < (g - r)_0 < 1.2$, respectively.

Using the SEGUE Stellar Parameter Pipeline (Allende Prieto et al. 2008; Lee et al. 2008a, 2008b), we estimated stellar atmospheric parameters (T_{eff} , $\log g$, and $[\text{Fe}/\text{H}]$) for each star. In order to obtain reliable stellar-parameter estimates for MS and MS turnoff (MSTO) stars, we restrict our analysis to stars

with average spectral signal-to-noise ratios (S/Ns) greater than 10.0, $4400 \leq T_{\text{eff}} \leq 7000$ K, and $\log g \geq 3.5$. For stars with multiple observations, we chose the star with the highest S/N, and removed stars with apparently defective spectra.

Proper motions for stars with errors less than 1.0 mas yr^{-1} were obtained through cross-matching with Gaia DR2 (Gaia Collaboration et al. 2018). Radial velocities were adopted from the SDSS pipeline; these have a precision of $5\text{--}20 \text{ km s}^{-1}$, depending on the S/N of the spectrum, and negligible zero-point errors (Yanny et al. 2009). For stellar-distance estimates, we employed the methods of Beers et al. (2000, 2012), as our program stars are mostly too faint to have reliable parallaxes available from Gaia DR2. Their reported uncertainty is on the order of 15%–20%, as verified by comparing our derived distances with Gaia DR2 distances based on parallaxes with relative errors less than 10% (Kim et al. 2019; Lee et al. 2019).

3. Space Velocity Components and Orbital Parameters

Given the distances, radial velocities, and proper motions adopted for our sample of stars, we derived their space velocity components in a spherical coordinate system. For these calculations, we adopted $V_{\text{LSR}} = 236 \text{ km s}^{-1}$ (Kawata et al. 2019) for the rotation of the local standard of rest (LSR), a solar position of $R_{\odot} = 8.2 \text{ kpc}$ (Bland-Hawthorn & Gerhard 2016) in the disk plane from the Galactic center, and a vertical distance of $Z_{\odot} = 20.8 \text{ pc}$ (Bennet & Bovy 2019) from the midplane. The solar peculiar motion with respect to the LSR was assumed to be $(U, V, W)_{\odot} = (-11.10, 12.24, 7.25) \text{ km s}^{-1}$ (Schönrich et al. 2010), where the velocity components U , V , and W are positive in the direction toward the Galactic anticenter, Galactic rotation, and north Galactic pole, respectively. In our adopted system, a star with $V_{\phi} > 0 \text{ km s}^{-1}$ has a prograde motion; retrograde rotation is indicated by $V_{\phi} < 0 \text{ km s}^{-1}$. Stars with $V_r > 0 \text{ km s}^{-1}$ move away from the Galactic center, and stars with $V_{\theta} > 0 \text{ km s}^{-1}$ move toward the south Galactic pole.

We also made use of a Galactocentric Cartesian reference frame, denoted by (X, Y, Z) , where the axes are positive in orientation toward the Sun, Galactic rotation, and north Galactic pole, respectively. In addition, we introduced an angle (α) between the orientation of the total angular momentum vector and the L_Z axis, and a position angle (Θ) of L_{\perp} measured from the negative L_X axis to the positive L_Y -axis direction of the angular momentum component in the X – Y plane. These are defined by:

$$\alpha = \cos^{-1}\left(\frac{L_Z}{L}\right) \text{ and } \Theta = \tan^{-1}\left(-\frac{L_Y}{L_X}\right),$$

where $L = \sqrt{L_{\perp}^2 + L_Z^2}$ is the total angular momentum, $L_{\perp} = \sqrt{L_X^2 + L_Y^2}$; L_X , L_Y , and L_Z are the X , Y , and Z components of the angular momentum, and are positive along the positive X -axis, the positive Y -axis, and the negative Z -axis directions, respectively. Schematic representations for α and Θ are shown in Figure 1. In this notation, stars with $L_Z > 0$ have prograde orbits and $\alpha < 90^\circ$. Retrograde orbits have $\alpha > 90^\circ$, and the inclination angle (i) of their orbital plane increases as α approaches 90° . For prograde motions, the inclination angle $i = \alpha$, whereas $i = 180^\circ - \alpha$ for retrograde orbits.

We employed an analytic Stäckel-type potential (see Chiba & Beers 2000; Kim et al. 2019 for details) in order to calculate

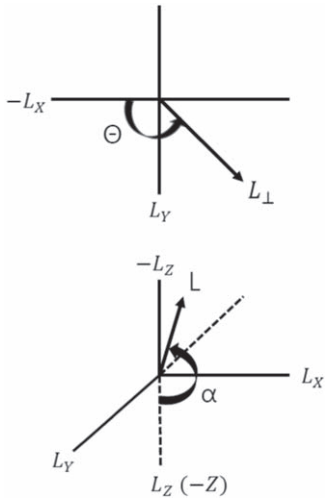


Figure 1. Top: position angle (Θ) of L_{\perp} , measured from the negative L_X axis to the positive L_Y -axis direction. Bottom: angle (α) between L and L_Z , measured from the positive L_Z axis.

the orbital parameters of our sample stars, including the perigalactic distance (r_{\min} , the minimum distance of an orbit from the Galactic center), apogalactic distance (r_{\max} , the maximum distance of an orbit from the Galactic center), and stellar orbital eccentricity ($e = (r_{\max} - r_{\min}) / (r_{\max} + r_{\min})$), as well as Z_{\max} (the maximum distance of a stellar orbit above or below the Galactic plane).

Uncertainties on the derived kinematic and orbital values are obtained from 100 Monte Carlo simulations with adopted uncertainties of 20% in distance, and quoted uncertainties in the radial velocity and proper motions, assuming Gaussian error distributions. Prior to examining the metallicity distribution function (MDF) of our program stars, we derived simple selection functions to correct for the target-selection bias. The selection function is defined by the fraction of the spectroscopically targeted stars among the photometrically available targets in bins of 0.2 and 0.05 mag for a color–magnitude diagram of r_0 and $g_0 - r_0$, separately for each SDSS plug-plate, as described in Lee et al. (2019).

Even though we obtained a total number of $N = 328,102$ stars with valid orbital parameters, in this study we focus on the lower metallicity stars with high-eccentricity orbits, in the range of $[\text{Fe}/\text{H}] < -1.0$ and $e > 0.7$, in order to reduce contamination from disk stars heated by the GSE (Belokurov et al. 2020), and include the GSE stars according to Mackereth et al. (2019), resulting in a total of 68,776 stars to be explored. Note that all of our selected stars are also included in the GSE even using the selection criteria by Naidu et al. (2020).

4. Results

In this section, we analyze the kinematic and orbital properties of stars with highly eccentric and radial orbits in two regions: the IHR ($15 \leq r_{\max} < 30$ kpc) and the OHR ($r_{\max} \geq 30$ kpc). In the IHR, we search for any differences in the dynamical properties between the LOI and HOI stars, while in the OHR, we explore the mean rotational velocity as a function of mean r_{\max} , and the stellar MDFs for the LOI and HOI populations.

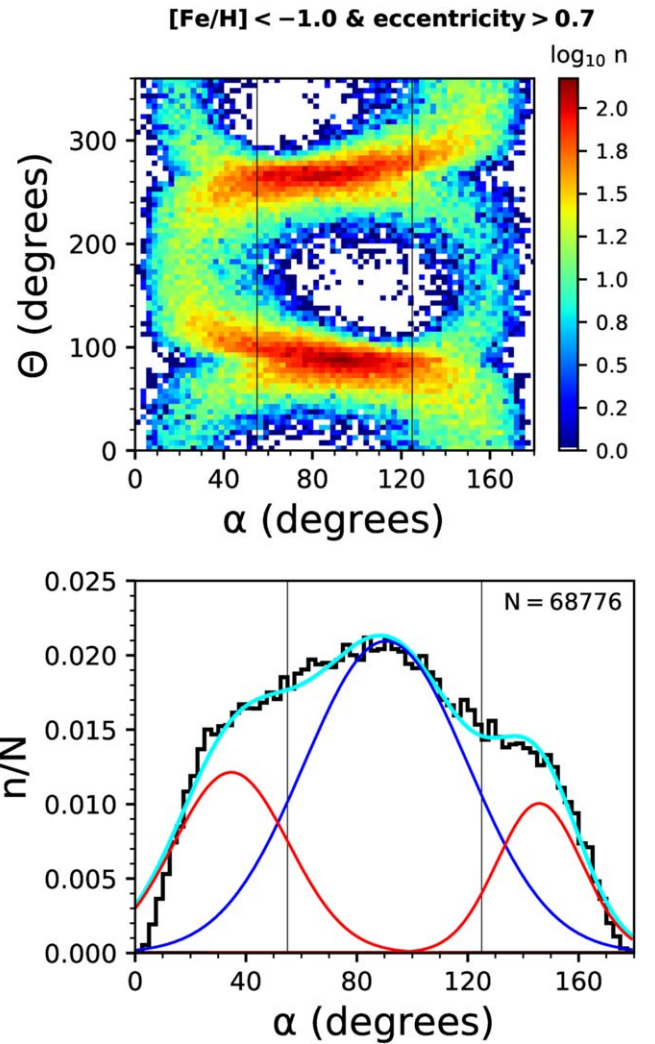


Figure 2. Top panel: map of the logarithmic number density in Θ vs. α for stars with $[\text{Fe}/\text{H}] < -1.0$ and $e > 0.7$. Bottom panel: histogram of α for our program stars (black line). The cyan solid line, which well-matches the black histogram, represents the sum of one normal distribution (blue) and two (red). The vertical lines in both panels are marked at $\alpha = 55^\circ$ and $\alpha = 125^\circ$, respectively.

4.1. Definition of LOI and HOI Populations

The top panel of Figure 2 presents the logarithmic number density of the selected program stars in the Θ versus α plane. In this map, we clearly see distinct kinematic features. Stars with relatively HOI of $55^\circ < \alpha < 125^\circ$ are mostly concentrated around $\Theta = 90^\circ$ and 270° , and have the highest density at $\alpha = 90^\circ$, whereas stars with relatively LOI of $\alpha \leq 55^\circ$ or $\alpha \geq 125^\circ$ are distributed over all ranges of Θ . Moreover, the α histogram (black color) for our program stars, shown in the bottom panel of Figure 2, is well-fit with the sum (cyan line) of three different Gaussian distributions, which represent one (blue) for the HOI and two (red) for the LOI population. By assembling these characteristics together, we define LOI stars as those in the range of $\alpha \leq 55^\circ$ or $\alpha \geq 125^\circ$; HOI stars are those in the range of $55^\circ < \alpha < 125^\circ$. The condition $55^\circ < \alpha < 125^\circ$ is equivalent to $L_{\perp}^2 / L^2 > \sin^2 55^\circ = 0.67$, or $L_{\perp} > \pm \tan 55^\circ L_Z = \pm 1.43 L_Z$ in the L_Z versus L_{\perp} space.

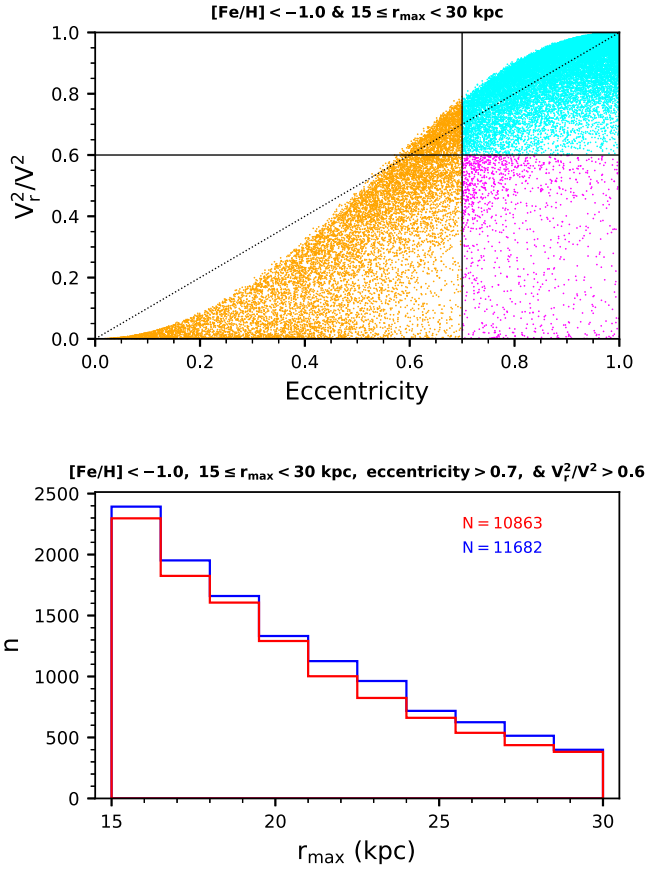


Figure 3. Top panel: distribution of V_r^2/V^2 vs. orbital eccentricity for stars with $[\text{Fe}/\text{H}] < -1.0$ and $15 \leq r_{\text{max}} < 30$ kpc. Cyan and magenta dots represent stars on radial and tangential orbits, respectively, with $e > 0.7$, while orange dots indicate stars with $e \leq 0.7$. Bottom panel: histograms of r_{max} for LOI (red) and HOI (blue) stars.

4.2. Separation of GSE Stars into Low and High Orbital-inclination Groups

First, in order to select GSE stars having highly eccentric and radial orbits in the IHR, we plot stars in the ranges of $15 \leq r_{\text{max}} < 30$ kpc (Deason et al. 2018) and $[\text{Fe}/\text{H}] < -1.0$ in the plane of V_r^2/V^2 versus orbital eccentricity, as shown in the top panel of Figure 3. In this figure, cyan, magenta, and orange dots represent stars with $e > 0.7$ on radial and tangential orbits, and stars with $e \leq 0.7$, respectively. Then, we choose GSE members (cyan dots in the panel), defined by $e > 0.7$ (Mackereth et al. 2019) and $V_r^2/V^2 > 0.6$ (Belokurov et al. 2018), where $V_r^2/V^2 > 0.6$ is equal to $\beta > 0.67$. The velocity anisotropy parameter (β) of each star is defined as $\beta = 1 - V_r^2/2V^2$ (see Binney & Tremaine 2008; Elias et al. 2020).

Next, we divide the GSE members into two groups of stars: the LOI and HOI subsamples, by following the definitions described in Section 4.1. The bottom panel of Figure 3 shows the r_{max} distribution of the LOI (red) and HOI (blue) populations, respectively. As can be seen, there are nearly equal numbers of stars for the LOI and HOI populations as a function of r_{max} . This indicates that their progenitor galaxies are likely different, as it is unlikely to have equal numbers of LOI and HOI stars if they are accreted from a single dwarf galaxy.

4.3. Inner-halo Region

The orange solid box in the top-right panel of Figure 4 indicates the GE stars identified in Helmi et al. (2018). We note in the panel that the GE stars in the box are mostly made up of LOI and HOI stars with retrograde motions. Furthermore, we can observe that the HOI stars (blue histogram) have mostly $e > 0.9$ in the bottom right panel of Figure 4, which is characteristic of the GS stars reported by Deason et al. (2018). Thus, we can confirm that most of our selected LOI (red dots) and HOI (blue dots) stars follow typical properties of the GSE stars in the E_{tot} versus L_z plane, although we applied slightly different selection criteria for the GSE member stars from the original works (e.g., Helmi et al. 2018). As a result, our selection criteria for the GSE members do not alter the interpretation of the dynamical properties of the genuine GSE stars.

The top-left panel of Figure 4 shows that the LOI and HOI subsamples have essentially identical distributions of V_r . However, the V_ϕ distribution (bottom left panel) and the e -distribution (bottom right panel) tell an entirely different story—the eccentricity distributions exhibit completely different behaviors between the LOI (red) and HOI (blue) populations. The LOI stars (red) are well-separated into two subgroups of prograde and retrograde motion in the V_ϕ distribution, and the LOI group mainly occupies the range of $e < 0.9$, while the majority of stars in the HOI population have $e > 0.9$. These properties provide clear evidence that these stars have experienced different accretion episodes. The HOI stars (blue) have almost zero net rotational velocity, suggesting that they share a common progenitor.

We can use other orbital parameters, e.g., Z_{max} and r_{max} , to explore more the discrete dynamical signatures of the LOI and HOI populations. To accomplish this, we first introduce an angle, $\phi = \tan^{-1}(Z_{\text{max}}/\sqrt{r_{\text{max}}^2 - Z_{\text{max}}^2})$. As illustrated in the top panel of Figure 5, which shows the distribution in Z_{max} versus $\sqrt{r_{\text{max}}^2 - Z_{\text{max}}^2}$ for LOI (red dots) and HOI (blue dots) stars on highly eccentric and radial orbits, this angle is measured from the axis of $\sqrt{r_{\text{max}}^2 - Z_{\text{max}}^2}$ to a line connecting the origin to a star in the coordinate plane of $\sqrt{r_{\text{max}}^2 - Z_{\text{max}}^2}$ and Z_{max} . Generally, this angle (ϕ) increases with increasing Z_{max} at a given r_{max} (or E_{tot}).

The middle and bottom panels of Figure 5 show the distributions of the ϕ angles for LOI (red) and HOI (blue) stars, in the two regions of r_{max} : all r_{max} (middle panel) and $15 \leq r_{\text{max}} < 30$ kpc (bottom panel). These panels immediately indicate that the HOI stars have mostly higher ϕ values than those of the LOI stars, both over all r_{max} and $15 \leq r_{\text{max}} < 30$ kpc ranges. Once again, this discrepancy suggests a dynamical distinction between the two populations. One can assume that if both HOI and LOI stars were accreted from a relatively massive dwarf galaxy, as claimed in the literature (e.g., Belokurov et al. 2018; Helmi et al. 2018), no matter what the orbital inclination they have, both groups of stars should exhibit similar ϕ distributions, regardless of their r_{max} .

4.4. Outer-halo Region

We now extend our search for diverse dynamical signatures between LOI and HOI stars to the OHR, the region with $r_{\text{max}} \geq 30$ kpc. Once again, we only consider stars with

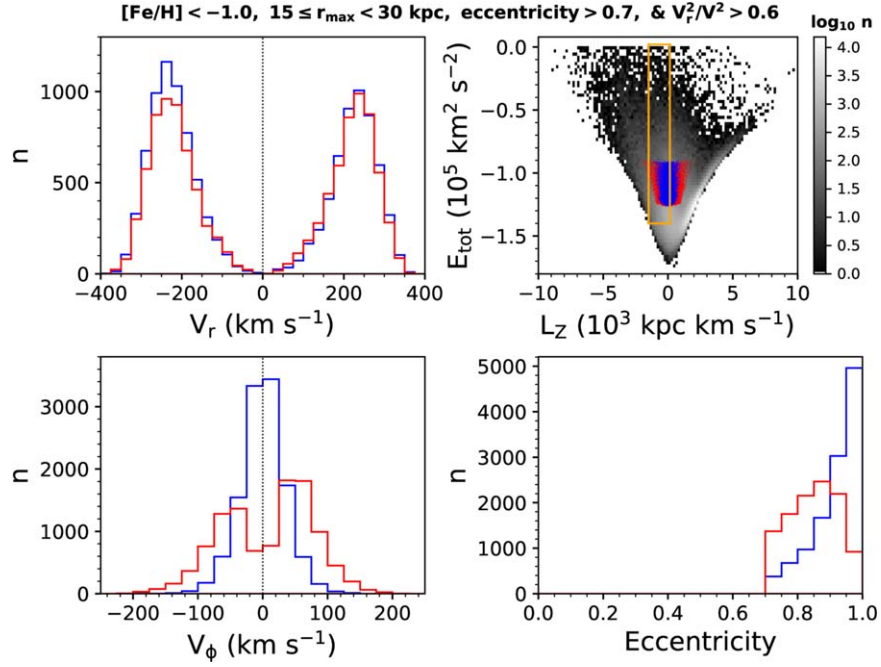


Figure 4. Left column: velocity distributions of V_r and V_ϕ for LOI (red) and HOI (blue) stars, in the top and bottom rows, respectively. Right column: same as in the left column, but for distributions of total energy (E_{tot}) vs. L_z (number densities are shown on a \log_{10} scale with gray color as indicated in the bar), and orbital eccentricity, in the top and bottom rows, respectively. An orange solid box in the top-right panel marks the location of GE by Helmi et al. (2018), scaled to the Galactic potential used by this study.

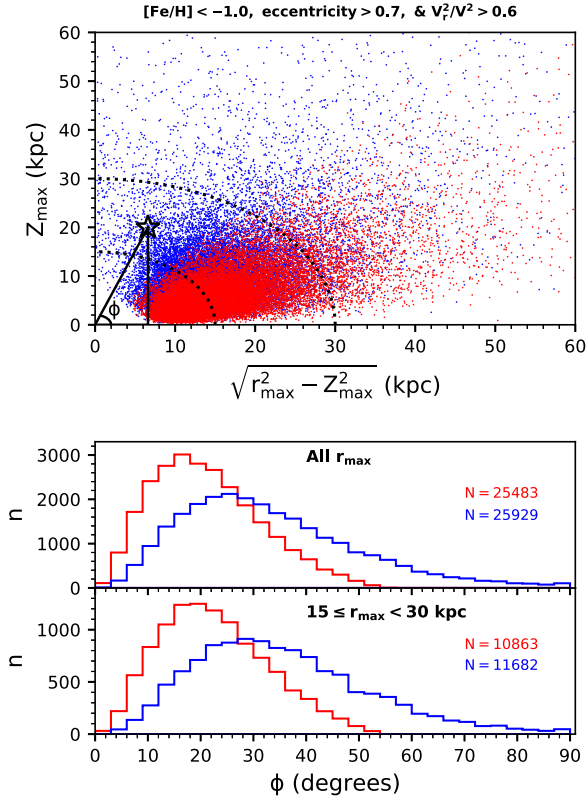


Figure 5. Top panel: distribution in Z_{max} vs. $\sqrt{r_{\text{max}}^2 - Z_{\text{max}}^2}$ for LOI (red dots) and HOI (blue dots) stars on highly eccentric and radial orbits among our program stars. Inner and outer dotted curves show $r_{\text{max}} = 15$ and 30 kpc, respectively. The right triangle is the schematic diagram for the definition of an angle, $\phi = \tan^{-1}(Z_{\text{max}}/\sqrt{r_{\text{max}}^2 - Z_{\text{max}}^2})$. Middle panel: distributions of ϕ for LOI (red) and HOI (blue) stars over the full range of r_{max} . Bottom panel: same as in the middle panel, but for $15 \leq r_{\text{max}} < 30$ kpc.

$[\text{Fe}/\text{H}] < -1.0$ on highly eccentric ($e > 0.7$) orbits, and apply the selection criteria for LOI and HOI stars described in Section 4.1 to the OHR. First, we search for evidence of retrograde motions and dissimilar MDFs for stars in the OHR. The left plot of top panels in Figure 6 shows the profiles of mean rotation velocity, as a function of r_{max} , for the full sample of stars (brown), and for stars with $V_r^2/V^2 > 0.6$ (black). The middle plot shows the V_ϕ distributions for stars with $r_{\text{max}} \geq 30$ kpc. The right plot represents the MDFs for the stars with $r_{\text{max}} \geq 30$ kpc and $V_\phi < 0$ km s $^{-1}$. The black and magenta histogram in the middle and right plots in each panel denote stars with $V_r^2/V^2 > 0.6$ (radial-motion dominated) and $V_r^2/V^2 \leq 0.6$ (tangential-motion dominated), respectively. Plots in the top panels are for the LOI population, whereas bottom panels are the same as in the top panels, but for the HOI population.

Inspection of the left plot of the top panels shows that the LOI stars with strong radial motions (black) exhibit stronger retrograde motions in the OHR than in the IHR, and drops down to $V_\phi \sim -70$ km s $^{-1}$ at $r_{\text{max}} \sim 75$ kpc. This behavior can also be inferred from the V_ϕ distribution (black histogram) in the middle plot, which presents more stars with retrograde motion than in prograde motion. By way of contrast, the HOI group of stars with strong radial motion (black) in the left plot of bottom panels exhibits a small retrograde motion, $V_\phi \sim -15$ km s $^{-1}$, in the OHR, and does not change with increasing r_{max} up to ~ 85 kpc. The middle plot indicates that their V_ϕ distribution (black histogram) appears to be symmetric around $V_\phi \sim 0$ km s $^{-1}$. As a result, we realize that the behaviors in the V_ϕ distributions for both LOI and HOI stars with $V_r^2/V^2 > 0.6$ in the OHR are not much different in the IHR. One more interesting aspect is that we generally see a steeper gradient (brown) of V_ϕ over r_{max} in the OHR in the left plot of top and

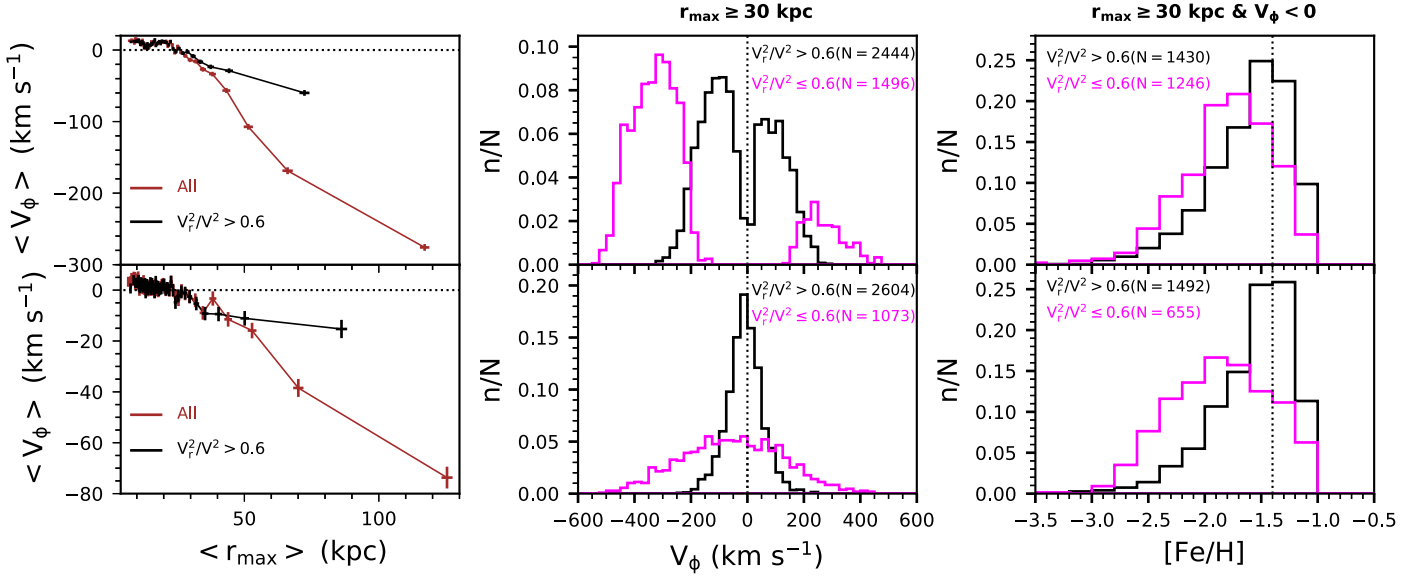


Figure 6. Top panels: from left to right, profiles of mean rotational velocity, as a function of mean r_{\max} , for the full sample (brown color) and for stars having $V_r^2/V^2 > 0.6$ (black), distributions of rotational velocity for stars with $r_{\max} \geq 30$ kpc, and MDFs for stars in ranges of $r_{\max} \geq 30$ kpc and $V_\phi < 0$ for LOI stars with $[\text{Fe}/\text{H}] < -1.0$ and $e > 0.7$. Bottom panels: same as in top panels, but for HOI stars. In both panels, each mean value is obtained by passing a box of 500 stars in r_{\max} . The error bars on V_ϕ are obtained from 100 Monte Carlo samples. The black and magenta histograms in the V_ϕ distributions and MDFs represent stars separated into $V_r^2/V^2 > 0.6$ and $V_r^2/V^2 \leq 0.6$, respectively.

bottom panels. This is driven by the stars on the tangential orbits ($V_r^2/V^2 \leq 0.6$) with retrograde motion.

We now examine the MDF of stars with retrograde motions in the OHR. From the right plot of top and bottom panels of Figure 6, one can clearly see different MDFs between the radial- and tangential-dominated samples for the LOI and HOI stars. The peaks of the MDFs for LOI stars on highly radial and tangential orbits are at $[\text{Fe}/\text{H}] = -1.5$ and -1.7 , respectively, while the peaks of the HOI stars are at $[\text{Fe}/\text{H}] = -1.3$ and -1.9 , respectively. Converting to the stellar masses of their progenitors by the mass–metallicity relationship for dwarf galaxies (Kirby et al. 2013), we obtained $M_* \sim 2 \times 10^6 M_\odot$ and $M_* \sim 4 \times 10^5 M_\odot$ for LOI stars, and $M_* \sim 3 \times 10^6 M_\odot$ and $M_* \sim 3 \times 10^5 M_\odot$ for HOI stars, respectively. Similarly, the stellar mass for the progenitor of the LOI stars with prograde motion on highly radial orbits is $M_* \sim 3 \times 10^6 M_\odot$. Consequently, the discrepancies in the MDFs and progenitor masses suggest that the progenitor of the stars on highly radial orbits experienced different star formation histories from that of those on tangential orbits, for both the LOI and HOI subsamples.

5. Discussion

In the previous section, we showed that the LOI and HOI stars in the IHR exhibit different distributions in V_ϕ , e , and the ϕ angle. The LOI stars include more objects with $e < 0.9$ and small ϕ angles, and they are well-separated into stars with prograde and retrograde motions. On the other hand, the HOI stars have more objects with $e > 0.9$ and high ϕ angles, and they exhibit a single V_ϕ -distribution with a peak at $V_\phi \sim 0$ km s⁻¹.

For stars in the OHR, the objects with tangential orbits among the LOI population exhibit stronger retrograde motions than the HOI population. Considering the stars with retrograde motions in the OHR, the tangential-dominated sample exhibits a more metal-poor distribution than the radial-dominated one for both the LOI and HOI populations.

How do we interpret our findings in terms of the accretion history of the Galactic halo? Let us first consider the dynamical signatures of merging galaxies predicted from various numerical simulations. It is well-known that tidally stripped stars follow the orbital trajectories of their parent galaxies when they are fully accreted into the MW (e.g., Quinn & Goodman 1986; Van den Bosch et al. 1999; Amorisco 2017)—the accreted stars preserve the orbital eccentricity (Mackereth et al. 2019) and inclination (Re Fiorentin et al. 2015) of their parent galaxies. Numerical simulations also predict stars with retrograde motions in the OHR of a galaxy, accreted not only from the merging of two massive dwarf galaxies with different orbital directions on highly eccentric and low-inclination orbits (Murante et al. 2010), owing to the dissimilar efficacy of dynamical friction (Quinn & Goodman 1986), but also from one merged dwarf galaxy on a retrograde orbit of low inclination (Bignone et al. 2019). In terms of the spatial distribution of accreted stars, stars of a low-mass dwarf galaxy under the influence of very weak dynamical friction are tidally stripped off in the outer region of the MW, but its high eccentricity causes its stars to be deposited in the inner region of the MW (Karademir et al. 2019), whereas, due to stronger dynamical friction, a more-massive dwarf galaxy loses its stars in the inner region of the MW (Amorisco 2017).

Following the above reasoning, we can infer that our LOI stars on highly eccentric and radial orbits may be accreted from two massive dwarf galaxies with highly eccentric and low-inclination orbits in prograde and retrograde motions, respectively. Stars stripped from them might drive the prograde motion in the IHR and retrograde motion in the OHR, due to different dynamical friction efficacy arising from the different orbital directions. On the other hand, the HOI stars on highly eccentric and radial orbits are regarded as tidally stripped ones from one massive dwarf galaxy merged on an extremely eccentric and high-inclination orbit under the influence of dynamical friction.

Meanwhile, the LOI and HOI stars with retrograde motions on highly eccentric and tangential orbits have the peaks of their

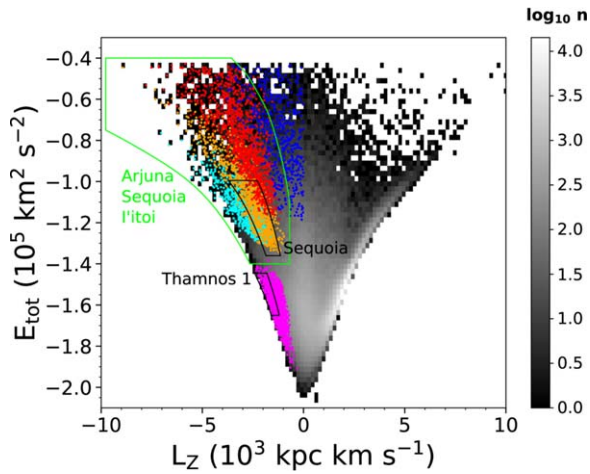


Figure 7. Distribution in E_{tot} vs. L_z for stars of previously identified substructures. Here we considered only stars with retrograde motions. Our LOI and HOI stars are displayed in red and blue colors, respectively. The Sequoia event, with $0.5 < e \leq 0.7$, $V_r^2/V^2 \leq 0.45$, and $r_{\text{max}} \geq 20$ kpc and Thamnos 1, with $e \leq 0.3$ and $r_{\text{max}} < 12$ kpc, are represented with orange and magenta colors, respectively. The cyan color marks substructures with $e \leq 0.5$ and $r_{\text{max}} \geq 20$ kpc, similar to those reported by Naidu et al. (2020). The green solid box indicates the area where the Arjuna, Sequoia, and I'toi substructures noted by Naidu et al. (2020) are located. Similarly, black solid boxes mark the region of Sequoia and Thamnos 1 by Koppelman et al. (2019).

MDFs located in the more metal-poor regime in the OHR than the radial-dominated stars. In addition, many of those stars have higher E_{tot} than stars on radial orbits. These aspects lead us to conclude that they may be stripped in the OHR of the MW, due to weak dynamical friction and self-gravity from low-mass dwarf galaxies that are on low- and high-inclination orbits with high eccentricity and retrograde motion at high E_{tot} , resulting in stripped stars that have large r_{max} . Taken as a whole, accounting for the dynamical characteristics of our LOI and HOI stars require at least five different accretion episodes.

To demonstrate that the LOI and HOI stars we analyze are different entities from other known substructures, we compared our two groups (LOI and HOI) of stars to those on retrograde orbits identified in the literature (Koppelman et al. 2019; Myeong et al. 2019; Naidu et al. 2020) in the L_z - E_{tot} diagram shown in Figure 7. The figure is drawn with the stars with $r_{\text{max}} < 200$ kpc, calculated using the McMillan (2017) potential for easy comparison with those in the literature. Substructures of stars in the LOI and HOI subsamples we have identified are represented in red and blue colors, respectively. The Sequoia event, with $0.5 < e \leq 0.7$, $V_r^2/V^2 \leq 0.45$, and $r_{\text{max}} \geq 20$ kpc, and Thamnos 1, with $e \leq 0.3$ and $r_{\text{max}} < 12$ kpc, are displayed with orange and magenta colors, respectively. The cyan color marks subsamples with $e \leq 0.5$ and $r_{\text{max}} \geq 20$ kpc, similar to those reported by Naidu et al. (2020). From inspection, our LOI and HOI stars on retrograde motions are clearly well-separated from the other known substructures.

6. Summary

Using metallicities, radial velocities, and distances from SDSS DR12 and proper motions from Gaia DR2, we have presented an analysis of the kinematic and orbital properties for MS and MSTO stars with eccentricities greater than 0.7 and $[\text{Fe}/\text{H}] < -1.0$, which are the typical properties of the GSE stars, after separating them into LOI and HOI subsamples.

LOI and HOI stars on highly eccentric and radial orbits exhibit different dynamical characteristics. LOI stars mostly have $e < 0.9$ and lower Z_{max} , whereas HOI stars have $e > 0.9$ and higher Z_{max} . Moreover, LOI stars are separated into two groups with prograde and retrograde motions, and exhibit prograde motions in the inner halo and retrograde motions in the outer halo. Accordingly, they are regarded as stars accreted from two massive dwarf galaxies with prograde and retrograde orbits of low inclination under the influence of different dynamical friction due to different orbital directions. On the other hand, HOI stars globally have a symmetric distribution of rotational velocity near zero, although they exhibit a small retrograde motion of $V_\phi \sim -15$ km s $^{-1}$ in the outer halo. These stars are considered to be stripped from a massive dwarf galaxy on a orbit of high inclination, based on their MDF with a peak of $[\text{Fe}/\text{H}] = -1.3$.

In addition, our analysis indicates that at least two low-mass progenitors are required to explain the distinct MDFs and dynamical properties between the LOI and HOI stars that are on retrograde motion with highly eccentric and tangential orbits in the OHR.

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